

Notes - Dimensional Analysis

It's all about cancelling units!

Roadmap $\xrightarrow{\text{given unit}} \dots \xrightarrow{\text{desired unit}}$

Skeleton $\frac{\text{Given unit}}{1} \times \frac{\text{unit}}{\text{unit}}$

Ex 1: How many seconds are in 3 hours?

Roadmap hours \rightarrow min \rightarrow seconds

$$\frac{3 \text{ hours}}{1} \times \frac{60 \text{ min}}{1 \text{ hour}} \times \frac{60 \text{ sec}}{1 \text{ min}} = \frac{10,800}{1} = 10,800 \text{ sec}$$

Ex 2: How many cm in 0.5 miles?

Miles \rightarrow feet \rightarrow inches \rightarrow cm

$$\frac{0.5 \text{ miles}}{1} \times \frac{5,280 \text{ ft}}{1 \text{ mile}} \times \frac{12 \text{ in}}{1 \text{ ft}} \times \frac{2.54 \text{ cm}}{1 \text{ in}} = 80,467.2 \text{ cm}$$

Ex 3: Convert 5 mph to cm/sec

miles \rightarrow ft \rightarrow in \rightarrow cm

hr \rightarrow min \rightarrow sec

$$\frac{5 \text{ miles}}{1 \text{ hr}} \times \frac{5,280 \text{ ft}}{1 \text{ mile}} \times \frac{12 \text{ in}}{1 \text{ ft}} \times \frac{2.54 \text{ cm}}{1 \text{ in}} \times \frac{1 \text{ hr}}{60 \text{ min}} \times \frac{1 \text{ min}}{60 \text{ sec}}$$

distance miles \rightarrow cm time hr \rightarrow sec

$$= \frac{804672 \text{ cm}}{3600 \text{ sec}} = 223.52 \text{ cm/sec}$$